

## Weighted Distance-Two Edge-Balance Index Sets of Star Graphs

Catello Battinelli\*, Hsin-Hao Su, Heiko Todt and Matthew Young, Stonehill College.

Let  $G$  be a simple graph with vertex set  $V(G)$  and edge set  $E(G)$ , and let  $\mathbb{Z}_2 = \{0, 1\}$ . Any edge labeling  $f$  induces a partial vertex labeling  $f^+ : V(G) \rightarrow \mathbb{Z}_2$  assigning 0 or 1 to  $f^+(v)$ ,  $v$  being an element of  $V(G)$ , depending on whether there are more 0-edges or 1-edges within the distance 2 to  $v$  where the counting of the number of edges is weighted by its distance to  $v$ , and no label is given to  $f^+(v)$  otherwise. For each  $i \in \mathbb{Z}_2$ , let  $v_f(i) = |\{v \in V(G) : f^+(v) = i\}|$  and let  $e_f(i) = |\{e \in E(G) : f(e) = i\}|$ . An edge-labeling  $f$  of  $G$  is said to be edge-friendly if  $|e_f(0) - e_f(1)| \leq 1$ . The weighted distance-two edge-balance index set of the graph  $G$  is defined as  $\text{WEBI}(G) = \{|v_f(0) - v_f(1)| : f \text{ is edge-friendly.}\}$ . In this paper, exact values of the weighted distance-two edge-balance index sets of stars are presented.

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