Weighted Distance-Two Edge-Balance Index Sets of Cycle Graphs

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Let G be a simple graph with vertex set $V(G)$ and edge set $E(G)$, and let $\mathbb{Z}_2 = \{0, 1\}$. Any edge labeling f induces a partial vertex labeling $f^+ : V(G) \to \mathbb{Z}_2$ assigning 0 or 1 to $f^+(v)$, v being an element of $V(G)$, depending on whether there are more 0-edges or 1-edges within the distance 2 to v where the counting of the number of edges is weighted by its distance to v, and no label is given to $f^+(v)$ otherwise. For each $i \in \mathbb{Z}_2$, let $v_f(i) = |\{v \in V(G) : f^+(v) = i\}|$ and let $e_f(i) = |\{e \in E(G) : f(e) = i\}|$. An edge-labeling f of G is said to be edge-friendly if $\{|e_f(0) - e_f(1)| \leq 1$. The weighted distance-two edge-balance index set of the graph G is defined as $\text{WEBI}(G) = \{|v_f(0) - v_f(1)| : f$ is edge-friendly.$\}$. In this paper, exact values of the weighted distance-two edge-balance index sets of cycles are presented.

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